

## Group

A non-empty set  $G$  of some elements ( $a, b, c$ , etc.), with one or more operations is known as a group.

A set needed to be satisfied following properties to become a group:

1) Closure Property:

$$a.b \in G, \forall a, b \in G$$

2) Associative Property:

$$(a . b) . c = a . (b . c), \forall a, b, c \in G$$

3) Existence of Identity:

$e \rightarrow$  identity element

$$e.a = a = a.e, \forall a \in G$$

4) Existence of Inverse:

$a^{-1} \rightarrow$  inverse of  $a$

$$a.a^{-1} = e = a^{-1}.a, \forall a \in G$$

## Abelian or Commutative Group

A set needed to be satisfied following properties to become an abelian group:

1) Closure Property:

$$a.b \in G, \forall a, b \in G$$

2) Associative Property:

$$(a \cdot b) \cdot c = a \cdot (b \cdot c), \forall a, b, c \in G$$

3) Existence of Identity:

$e \rightarrow$  identity element

$$e \cdot a = a = a \cdot e, \forall a \in G$$

4) Existence of Inverse:

$a^{-1} \rightarrow$  inverse of  $a$

$$a \cdot a^{-1} = e = a^{-1} \cdot a, \forall a \in G$$

5) Commutativity:

$$a \cdot b = b \cdot a, \forall a, b \in G$$

## Subgroup

A subgroup is a subset  $H$  of group elements of a group  $G$  that satisfies all the four properties of a group.

“ $H$  is a subgroup of  $G$ ” can be written as  $H \subseteq G$

A subgroup  $H$  of a group  $G$ , where  $H \neq G$ , is known as proper subgroup of  $G$ .