

Prove that $G = \{-1, 1, i, -i\}$ is a group under multiplication.

First need to show that G is indeed closed under the operation $*$

we have $1 * 1 = 1$ where $1 \in G$

we have $-1 * -1 = 1$ where $1 \in G$

we have $1 * -1 = -1$ where $-1 \in G$ and $-1 * 1 = -1 \in G$

we have $1 * i = i$ and $i * 1 = i$ where $i \in G$

we have $-1 * i = -i$ and $i * -1 = -i$ where $-i \in G$

let $k \in \mathbb{N}$ then $i^{2k} = -1$ where $-1 \in G$

Finally let $k \in \mathbb{N}$ then we have $i^{2k+1} = -i$ where $-i \in G$

So, all possible outcomes from every combination of multiplication between any elements yields an element in G .

Related posts:

1. Group
2. Undirected Graph and Incident Matrix
3. Prove the following by using the principle of mathematical induction for all $n \in \mathbb{N}$, $1^3 + 2^3 + 3^3 + \dots + n^3 = [n(n+1)/2]^2$
4. Hasse diagram for the "less than or equal to" relation on the set $S = \{0, 1, 2, 3, 4, 5\}$
5. SET
6. Mathematical induction

Prove that $G = \{-1, 1, i, -i\}$ is a group under multiplication.

7. Relation
8. Net 34
9. prove that- $A \cap (B \cap C) = (A \cap B) \cap (A \cap C)$
10. Prove that- $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
11. prove that - $(A \cap B) \cap (C \cap D) = (A \cap C) \cap (B \cap D)$
12. Show that- $(P \cap Q) \cap (R \cap S) = (P \cap R) \cap (Q \cap S)$
13. Binary operations
14. Algebraic structure
15. Show that $\{\dots, -4, -3, -2, -1, 0, 1, 2, 3, 4, \dots\}$ is group
16. Show that $a * b = b * a$
17. if $a * c = c * a$ and $b * c = c * b$, then $(a * b) * c = c * (a * b)$