

Prove that  $G=\{-1,1,i,-i\}$  is a group under multiplication.

First need to show that  $G$  is indeed closed under the operation  $*$

we have  $1*1=1$  where  $1 \in G$

we have  $-1*-1=1$  where  $1 \in G$

we have  $1*-1=-1$  where  $-1 \in G$  and  $-1*1=-1 \in G$

we have  $1*i=i$  and  $i*1=i$  where  $i \in G$

we have  $-1*i=-i$  and  $i*-1=-i$  where  $-i \in G$

let  $k \in \mathbb{N}$  then  $i^{2k}=-1$  where  $-1 \in G$

Finally let  $k \in \mathbb{N}$  then we have  $i^{2k+1}=-i$  where  $-i \in G$

So, all possible outcomes from every combination of multiplication between any elements yields an element in  $G$ .

## Related Posts:

1. Group
2. Undirected Graph and Incident Matrix
3. Prove the following by using the principle of mathematical induction for all  $n \in \mathbb{N}$ ,  $1^3 + 2^3 + 3^3 + \dots + n^3 = [n(n+1)/2]^2$
4. Hasse diagram for the "less than or equal to" relation on the set  $S = \{0,1,2,3,4,5\}$
5. SET
6. Mathematical induction
7. Relation

Prove that  $G = \{-1, 1, i, -i\}$  is a group under multiplication.

8. Net 34
9. prove that-  $A \cap (B \cap C) = (A \cap B) \cap (A \cap C)$
10. Prove that-  $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
11. prove that -  $(A \cap B) \cup (C \cap D) = (A \cup C) \cap (B \cup D)$
12. Show that-  $(P \cap Q) \cup (R \cap S) = (P \cup R) \cap (Q \cup S)$
13. Binary operations
14. Algebraic structure
15. Show that  $\{\dots, -4, -3, -2, -1, 0, 1, 2, 3, 4, \dots\}$  is group
16. Show that  $a * b = b * a$
17. if  $a * c = c * a$  and  $b * c = c * b$ , then  $(a * b) * c = c * (a * b)$